

1. Perform the operation  $3x^{\frac{3}{2}} \left( 3\sqrt{x} - \frac{8}{\sqrt{x}} \right)$  and simplify as much as possible.
2. Solve the nonlinear inequality  $x^2 > 3(x + 6)$ . Write your answer using interval notation.
3. Find all real solutions of  $\frac{3}{x-3} - \frac{6}{x^2} = 0$ . Write your answers as a comma-separated list. If there is no real solution write NO REAL SOLUTION and explain.
4. Find an equation of the line that passes through the points  $(4, 6)$  and  $(3, 8)$ .
5. Find and simplify the difference quotient  $\frac{f(a+h)-f(a)}{h}$ , where  $h \neq 0$  and  $f(x) = 6x^2 + 7$ .
6. A function is given.  $g(x) = \frac{5}{x}; x = 1, x = a$ 
  - (a) Determine the net change between the given values of the variable.
  - (b) Determine the average rate of change between the given values of the variable.
7. Sketch the graph of the piecewise defined function

$$f(x) = \begin{cases} 4 & \text{if } x \leq -1, \\ x^2 + 1 & \text{if } x > -1 \end{cases}$$

8. Sketch the graph of the function  $f(x) = -|x - 1|$ , not by plotting points, but by starting with the graph of a standard function and applying transformations.
9. Use the Inverse Function Property to determine whether  $f$  and  $g$  are inverses of each other.  $f(x) = \frac{1}{x-12}, x \neq 12$ ; and  $g(x) = \frac{1}{x} + 12, x \neq 0$  Explain your answer.
10. Sketch the graph of the function  $f(x) = -x^2 + 4x - 3$ . Find the coordinates of the vertex and the x- and y- intercepts.
11. A polynomial function is given  $g(x) = -x^3 + 3x^2$ . Describe the end behavior of  $g$  and sketch its graph. Label all x- and y- intercepts on your graph.
12. Evaluate  $\log_3\left(\frac{1}{27}\right)$ .
13. Solve  $4 - \log(7 - x) = 3$  for x.
14. Graph the function  $y = 3^{(x-3)} - 1$ , not by plotting points but by transforming the graph of a more basic function. Show and label all intercepts and asymptotes.
15. Find the exact value of  $\sin\left(\frac{29\pi}{6}\right)$ .
16. Find  $\cos \theta$  if  $\sin \theta = -\frac{4}{5}$  and  $\theta$  is in quadrant IV.
17. Sketch the graph of two complete periods of the function  $y = -5 \sin(\pi x)$ . Label all intercepts, maximums, and minimums.
18. Find  $\tan\left(\sin^{-1}\left(-\frac{1}{2}\right)\right)$ .
19. Verify the identity  $(1 - \sin^2 x)(1 + \tan^2 x) = 1$ .
20. Find all solutions to the equation  $\sqrt{2} \cos t - 1 = 0$  for t in the interval  $-\pi \leq t \leq \pi$ .