## 1 Do five of the following six problems: 1-6

1. Prove the trigonometric identity $\frac{\sin 2 x}{1+\cos 2 x}=\tan x$.
2. Simplify $\frac{x+3}{4 x^{2}-9} \div \frac{x^{2}+7 x+12}{2 x^{2}+7 x-15}$.
3. Rewrite without parentheses or a radical $\operatorname{sign} y^{\frac{3}{5}}\left(\sqrt{y}-\frac{1}{\sqrt{y}}\right)$.
4. Solve $\frac{5}{x+2}-\frac{6}{x}+1=0$ for x .
5. Find all x that solve $x^{3}>x^{2}$.
6. Given $f(x)=2 x-4 x^{2}$. Find and simplify
(a) $f(3-a)$
(b) $f\left(\frac{a}{2}\right)$

## 2 Do five of the following six problems: 7-12

7. Show that the equation $x^{2}+y^{2}+\frac{1}{2} x-2 y+\frac{1}{16}=0$ represents a circle, and find its center and radius.
8. Given $f(t)=t-2 t^{2}$. Find and simplify the average rate of change of f from $t=2$ to $t=2+h$.
9. Sketch the graph of the function $y=2-\sqrt{x+1}$. Label at least three points on your graph including any intercepts. Begin with $y=\sqrt{x}$ and indicate the steps needed to transform its graph to the graph of $y=2-\sqrt{x+1}$.
10. Given $f(x)=\frac{x}{x+1}$ and $g(x)=\frac{2}{x}$. Evaluate and simplify $f(g(7))-g(f(7))$.
11. Let

$$
f(x)=\left\{\begin{aligned}
1-2 x & \text { if } x \leq 1 \\
2 x & \text { if } x>1
\end{aligned}\right.
$$

(a) Evaluate $f(-2)$ and $f(1)$.
(b) Sketch the graph of $f(x)$ from $x=-3$ to $x=3$.
12. Sketch the graph of $p(x)=-x(x+2)^{2}(x-2)^{3}$. Label all intercepts and indicate the end behavior.

## 3 Do five of the following six problems: 13-18

13. A bacteria culture starts with 900 bacteria. After one hour the count is 1000 .
(a) Assuming that bacteria population grows exponentially, find a function that models the number of bacteria $n(t)$ after thours. (You may leave $e, \log$, or $\ln$ in your answer).
(b) After how many hours will the number of bacteria double? (You may leave $e$, log, or ln in your answer).
14. Given the function $f(x)=2-x^{3}$.
(a) Sketch the graph of $f$.
(b) Find the formula for the inverse function $f^{-1}(x)$.
15. For the graph of the function in Figure 1, determine the interval(s) on which the function is increasing.
16. Solve for t in each of the following parts. You may leave $e, \log$, or $\ln$ in your answer.


Figure 1:
(a) $5 e^{2 t}-20=0$
(b) $3-\log (3-x)=1$.
17. Evaluate $\log _{3}\left(\frac{1}{\sqrt{27}}\right)$.
18. Perform the subtraction $\frac{7}{x+6}-\frac{1}{x^{2}+8 x+12}$ and simplify.

## 4 Do five of the following six problems: 19-24

19. Find the exact value of $\tan \left(-\frac{20 \pi}{3}\right)$.
20. For $y=-3 \sin \left(x+\frac{\pi}{6}\right)$ find the amplitude, period, phase shift and then graph. Label the coordinates of three points on your graph: one maximum point, one minimum point and one intercept.
21. Find $\cos 105^{\circ}$.
22. Find all solutions $\theta$ to $6 \cos ^{2} \theta-3=0$ for $\theta$ in the interval $-\pi \leq \theta \leq \pi$.
23. Evaluate each of the following
(a) $\sin ^{-1}\left(\frac{\sqrt{2}}{2}\right)$
(b) $\arcsin \left(\sin \left(\frac{11 \pi}{6}\right)\right)$
24. Find the radius $r$ of the circle in Figure 2 with shaded angle of measure $\frac{1}{2}$ radians that is subtended by the arc s of length 6 .


Figure 2:

