

Math 392 Test 1B

March 27, 2019

Name: _____

Note that both sides of each page may have printed material.

If you could read the directions
before asking me a question



Instructions:

1. Read the instructions.
2. Panic!!! Kidding, don't panic! I repeat, **do NOT panic!** Don't look down, while you're at it.
3. Complete all problems.
4. Show **ALL** your work to receive full credit, unless otherwise stated. You will get 0 credit for simply writing down the answers.
5. Write neatly so that I am able to follow your sequence of steps and box your answers.
6. Read through the exam and complete the problems that are easy (for you) first!
7. You are NOT allowed to use notes, or other aids—including, but not limited to, divine intervention/inspiration, the internet, telepathy, knowledge osmosis, the smart kid that may be sitting beside you or that friend you might be thinking of texting.
8. In fact, **cell phones and watches should be out of sight! If I catch you with a cellphone or a watch, you will fail the exam. If I catch you with any other paper than this exam, you will fail the exam. No calculators.**
9. Use the correct notation and write what you mean! x^2 and $x2$ are not the same thing, for example, and I will grade accordingly.
10. Other than that, have fun and good luck!

Don't worry, this is gonna work



You're gonna pass this test

I know I am



'cuz I dunno what Imma do if I don't

1. Let $\mathbf{F} = \langle 2x \ln y - yz, \frac{x^2}{y} - xz, -xy \rangle$.

(a) Show that \mathbf{F} is conservative by finding a potential function, f , for \mathbf{F} . (15 points)

(b) Find the work done by \mathbf{F} in moving an object along the path C , where C is parametrized by two curves: the vector curve $\vec{r}(t) = \langle \cos t, t \sin t + 1, e^{t^2} \rangle$ from $(1,1,1)$ to $(-1,1,e^{\pi^2})$ (Note that $t = 0$ for the first point and $t = \pi$ for the second point), followed by the straight line segment from $(-1,1,e^{\pi^2})$ to $(1,1,0)$ (Remember how to parametrize line segments and how to set up the limits!!!). (5 points)

2. Compute $\int_C \sqrt{x} + y \, ds$, where C is the closed curve in the plane consisting of a parabolic arc along $x = y^2$ from $(0,0)$ to $(1,1)$, followed by a line segment from $(1,1)$ back to $(0,0)$. Include a sketch of C in your answer. (20 points)

3. Let S be the part of the surface $z = 1 - x^2$ in the first octant with $0 \leq y \leq 1$. Let C be the curve of intersection of S with the plane $y = 1$. If $\mathbf{F} = \langle x, y, x^2 \rangle$, find the work done by \mathbf{F} in moving a particle along the curve C ; assuming C is oriented so that the final point is in the xy -plane. (20 points)

4. Let R be the region in the second quadrant bounded by the circle of radius a , $y = 0$, and $x = 0$. Let C be the boundary curve of R , oriented *counter-clockwise*.

Compute $\oint_C xy \, dx - xy \, dy$ in two ways:

- (a) Directly as a line integral. (10 points)

(This is problem 4 recopied for your convenience. Do part (b) on this page!)

Let R be the region in the second quadrant bounded by the circle of radius a , $y = 0$, and $x = 0$. Let C be the boundary curve of R , oriented *counter-clockwise*.

Compute $\oint_C xy \, dx - xy \, dy$ in two ways:

(b) As a double integral using Green's Theorem. (10 points)

5. Compute $\iint_S y \, dS$, where S is the portion of $z = x^2 + y^2$ in the first octant for $z \leq 1$. (10 points)

6. Let $\vec{F} = \langle y \cos x, z \ln y, x^2 yz \rangle$. Compute (5 points each):

(a) $\text{curl} \vec{F}$

(b) $\text{div} \vec{F}$

when you realize jhevon might drop even more quizzes,
so now you can radically improve your grade

REALITY CAN BE WHATEVER I WANT.



