## MATH 392 Quiz 2B

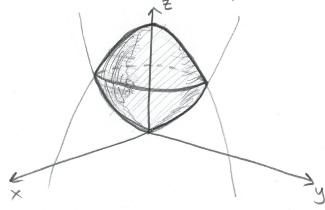
Instructions: No calculators! Use your own scrap paper and write your answers in the space provided.

1. Let  $\vec{r}(t) = \langle x(t), y(t), z(t) \rangle$ , f(x, y, z) be a scalar function, and  $P(x_1, y_1)$  and  $Q(x_2, y_2)$  be points in  $\mathbb{R}^2$ . Complete the following rules with vector functions:

(a) 
$$\vec{r}'(t) = (x'(t), y'(t), 2'(t))$$

(c) Line segment 
$$\overrightarrow{PQ} = (x_1 + (x_2 - x_1)t, y_1 + (y_2 - y_1)t)$$
  $(x_1 + (y_2 - y_1)t)$ 

2. (a) (2 points) Sketch the region bounded by  $z = 8 - x^2 - y^2$  and  $z = x^2 + y^2$ .



(b) Parametrize the curve of intersection,  $ec{r}_i(t)$ , of the above two surfaces. Set up the limits so that the curve is traversed once.

$$\vec{r}_i(t) = \langle 2\cos t, 2\sin t, 4 \rangle$$

- 3. (a) Parametrize the line segment from (-1,1,2) to (2,2,-3):  $\vec{r}_l(t) = \langle -1+3t, 1+t, 1-5t \rangle$ , 04 $t \leq 1$ 
  - (b) What is the length of the above line?  $L = \sqrt{35}$
- Find a unit vector that is orthogonal to both < -1,2,0 > and < 3,4,-2 >.  $\vec{u} = \sqrt{\frac{2}{120}}, \sqrt{\frac{2}{120}}, \sqrt{\frac{2}{120}}$ 四〈谎,谎,谎,

## **Bonus:**

- 1. Let  $C = \vec{r}(t)$  and f be as in problem 1. Find formulas for:
  - The length of  $\vec{r}(t)$  for  $a \le t \le b$ :  $L = \int_{a}^{b} (x'(t))^{2} + (y'(t))^{2} + (z'(t))^{2} dt$ (i)

(ii) 
$$\int_{C} f ds = \int_{a}^{b} f(x(t), y(t), z(t)) \cdot \sqrt{(x')^{2} + (y')^{2} + (z')^{2}} dt$$

2. Compute the length of  $\vec{r}(t) = <\sqrt{7}, \sin^2 t, \cos^2 t > \text{ for } 0 \le t \le \frac{\pi}{4}$ :

Integral Set-up:  $\sqrt{7}$  Sin2t of