Name: _

Final Exam

ID: _____

Answer each non-graph question CLEARLY on the provided line.

1. (4 points) Find the center and radius of the circle given by the equation $x^2 + y^2 + \frac{1}{2}x + 2y + \frac{1}{16} = 0$.

2. (4 points) Find all solutions t to $t^2 - 6t + 1 = 0$.

2._____

3. _____

1. _____

3. (4 points) Find all solutions θ to $2 \sec^2 \theta - 4 = 0$ for $0 \le \theta \le 2\pi$.

4. (4 points) Perform the addition and subtraction $\frac{2}{x} + \frac{3}{x-1} - \frac{4}{x^2-x}$ and simplify completely as one rational expression.

5. (4 points) Solve $\log(x) = 1 - \log(x - 3)$ for x.

6. (4 points) Evaluate $\tan^{-1}\left(\frac{-\sqrt{3}}{3}\right)$.

7. (4 points) Evaluate $\cos\left(-\frac{7\pi}{6}\right)$ radians.

7. _____

6. _____

5. _____

8. (4 points) Determine the average rate of change of $f(x) = x^3 - 5x^2$ between x = 5 and x = 10.

9. (4 points) The initial size of a bacteria culture is 1000. After one hour the bacteria count is 4000. After how many hours will the bacteria population reach 7000? Assume the population grows exponentially. (You may leave *e*, ln, or log in your answer.)

9. _____

10. (4 points) Solve $e^{3-5x} = 16$ for x. (You may leave e, ln, or log in your answer.)

10. _____

11. (4 points) Solve the inequality $\frac{x}{x+1} > 3$. Express your answer in interval notation.

11._____

12. (4 points) Simplify $\frac{f(a+h)-f(a)}{h}$ completely when $h \neq = 0$ and $f(x) = 3x^2 - 1$.

13. (4 points) Find $f^{-1}(x)$ when $f(x) = \frac{1}{x+3}$.

13. _____

14. (4 points) Find the range of $f(x) = -\frac{1}{2}x^2 - 2x + 6$.

14. _____



15. _____

16. (4 points) Evaluate $\cos\left(\frac{5\pi}{12}\right)$.

17. (4 points) Find $\cos(\theta)$ given that $\tan \theta = -\frac{4}{3}$ and θ is in Quadrant IV.

17. _____

18. (4 points) Sketch the graph of $F(x) = 25 - (x+5)^2$. Label vertex and all intercepts on your graph.

19. (4 points) Find an equation of the line passing through the points (-7,3) and (10,0).

19. _____

20. (4 points) Find all solutions x to $2 + \sqrt{9-x} = x - 5$.

21. (4 points) Evaluate $\log_2\left(\frac{1}{64}\right)$.

21. _____

22. (4 points) Sketch the graph $y = 2^{x-2} - 2$. Label all intercepts and asymptotes on your sketch.

23. (4 points) Sketch the graph $f(x) = -\log(x+6)$. Label all intercepts and asymptotes on your sketch. State the domain and range using interval notation.

24. (4 points) Sketch the graph of $f(x) = x^2(x^2 - 25)$.

25. (4 points) Sketch the graph $y = -2\tan(\frac{\pi x}{4})$.