

1. Use the Intermediate Value Theorem to show that  $f(x) = x^2 - \frac{1}{x} - 3$  has a root in the interval  $[1.5, 2]$ .
2. Suppose  $f(2) = 6$ , and  $0.4 \leq f'(x) \leq 0.5$  for  $x$  in  $[2, 2.2]$ . Use the MVT to estimate  $f(2.2)$ .
3. Consider  $f(x) = \frac{x}{x^2+1}$ . In which intervals does  $f$  increase. In which intervals does  $f$  decrease. Find the maximum and minimum values of  $f$  in  $[-10, 10]$ .
4. Find the maximum and minimum values of  $f(x) = 2x^3 - 3x^2 - 12x + 8$  on each of the following intervals,  $[-2.5, 4]$  and then  $[-2, 3]$  and then  $[-2.25, 3.75]$ .
5. Find the Taylor polynomials  $T_2(x)$  and  $T_3(x)$  for  $f(x) = 1 + x + x^2 + x^3 + x^4$  in powers of  $x$ .
6. Find the Taylor series for  $f(x) = \sin(3x)$  in powers of  $x$ .
7. Consider  $f(x) = \sqrt{x}$  on the interval  $1 \leq x \leq 1 + d$ . Find  $d$  small enough so that  $T_2(x)$  the second-degree Taylor polynomial at  $x = 1$ , approximates  $f(x)$  on  $[1, 1 + d]$  with an error at most 0.1 How about with an error .001?
8. Find the number(s)  $c$  referred to in the MVT for  $f(x) = \sqrt{x}$  over  $[0, 4]$ .
9. Use the onion method to evaluate  $P(3)$  when  $P(x) = x^4 + x^3 - 13x^2 - x - 12$ .
10. Find the relative and approximate error when  $w$  is used to approximate  $v$ .
  1.  $v = 2.71828182, w = 2.7182$
  2.  $v = 98350, w = 98000$
  3.  $v = .0000068, w = .000006$
11. Do end of Chapter 1 exercise in section 1.4 : 0, 1, 2, 3.