

2.2

use the methods shown in exercises 23-38 to evaluate #5.
#6 is mostly limit for the other Calculus sequence.

$$12) \lim_{t \rightarrow -1} (5t^2 - 3t + 2) = 5(-1)^2 - 3(-1) + 2 = 5(1) + 3 + 2 = \underline{\underline{10}}$$

$$14) \lim_{x \rightarrow 4} (3x - 9)^4 = (3(4) - 9)^4 = (12 - 9)^4 = (3)^4 = \underline{\underline{81}}$$

$$20) a) g(x) = \frac{x^2 - 3x - 4}{x + 1} \quad \begin{array}{l} x + 1 = 0 \\ x = -1 \end{array} \quad \text{domain: } (-\infty, -1) \cup (-1, \infty)$$

$$b) \lim_{x \rightarrow 3} g(x) = \lim_{x \rightarrow 3} \left(\frac{x^2 - 3x - 4}{x + 1} \right) = \frac{(3)^2 - 3(3) - 4}{(3) + 1} = \frac{9 - 9 - 4}{4} = \frac{-4}{4} = \underline{\underline{-1}}$$

$$c) \lim_{x \rightarrow -1} g(x) = \lim_{x \rightarrow -1} \left(\frac{x^2 - 3x - 4}{x + 1} \right) = \lim_{x \rightarrow -1} \left(\frac{(x+1)(x-4)}{x+1} \right) = \lim_{x \rightarrow -1} (x-4) = (-1) - 4 = \underline{\underline{-5}}$$

$$22) a) R(x) = \frac{x^2 - 2x - 8}{x^2 - 16} \quad \begin{array}{l} x^2 - 16 = 0 \\ (x+4)(x-4) = 0 \\ x+4=0 \quad | \quad x-4=0 \\ x=-4 \quad | \quad x=4 \end{array} \quad \text{domain: } (-\infty, -4) \cup (-4, 4) \cup (4, \infty)$$

$$b) \lim_{x \rightarrow 2} R(x) = \lim_{x \rightarrow 2} \left(\frac{x^2 - 2x - 8}{x^2 - 16} \right) = \frac{(2)^2 - 2(2) - 8}{(2)^2 - 16} = \frac{4 - 4 - 8}{4 - 16} = \frac{-8}{-12} = \underline{\underline{\frac{2}{3}}}$$

$$c) \lim_{x \rightarrow 4} R(x) = \lim_{x \rightarrow 4} \left(\frac{x^2 - 2x - 8}{x^2 - 16} \right) = \lim_{x \rightarrow 4} \left(\frac{(x+2)(x-4)}{(x+4)(x-4)} \right) = \lim_{x \rightarrow 4} \left(\frac{x+2}{x+4} \right) = \frac{(4)+2}{(4)+4} = \frac{6}{8} = \underline{\underline{\frac{3}{4}}}$$

$$24) \lim_{x \rightarrow -2} (4x^2 + x) = 4(-2)^2 + (-2) = 4(4) - 2 = 16 - 2 = \underline{\underline{14}}$$

$$26) \lim_{w \rightarrow 5} \frac{3w^2 + 1}{w} = \frac{3(5)^2 + 1}{(5)} = \frac{3(25) + 1}{5} = \frac{75 + 1}{5} = \underline{\underline{\frac{76}{5}}}$$

$$28) \lim_{x \rightarrow 4} \frac{x^2 - 4x}{x^2 - 3x - 4} = \lim_{x \rightarrow 4} \frac{x(x-4)}{(x+1)(x-4)} = \lim_{x \rightarrow 4} \frac{x}{x+1} = \frac{(4)}{(4)+1} = \underline{\underline{\frac{4}{5}}}$$

$$30) \lim_{x \rightarrow -4} \frac{x^2 + 5x + 4}{x^2 + 3x - 4} = \lim_{x \rightarrow -4} \frac{(x+4)(x+1)}{(x+4)(x-1)} = \lim_{x \rightarrow -4} \frac{x+1}{x-1} = \frac{(-4)+1}{(-4)-1} = \frac{-3}{-5} = \underline{\underline{\frac{3}{5}}}$$

$$32) \lim_{x \rightarrow -1} \frac{x^2 + 2x + 1}{x^2 - 1} = \lim_{x \rightarrow -1} \frac{(x+1)(x+1)}{(x^2+1)(x^2-1)} = \lim_{x \rightarrow -1} \frac{(x+1)(x+1)}{(x^2+1)(x+1)(x-1)}$$

$$= \lim_{x \rightarrow -1} \frac{x+1}{(x^2+1)(x-1)} = \frac{(-1)+1}{((-1)^2+1)((-1)-1)} = \frac{0}{(2)(-2)} = \frac{0}{-4} = \underline{\underline{0}}$$

$$34) \lim_{h \rightarrow 0} \frac{\sqrt{1+h} - 1}{h} = \lim_{h \rightarrow 0} \left(\frac{\sqrt{1+h} - 1}{h} \right) \left(\frac{\sqrt{1+h} + 1}{\sqrt{1+h} + 1} \right)$$

$$= \lim_{h \rightarrow 0} \left(\frac{(1+h) - (1)^2}{h(\sqrt{1+h} + 1)} \right) = \lim_{h \rightarrow 0} \frac{h}{h(\sqrt{1+h} + 1)}$$

$$= \lim_{h \rightarrow 0} \frac{1}{\sqrt{1+h} + 1} = \frac{1}{\sqrt{1+(0)} + 1} = \frac{1}{\sqrt{1} + 1}$$

$$= \frac{1}{1+1} = \underline{\underline{\frac{1}{2}}}$$

b > 0

$$\begin{aligned}
 36) \lim_{x \rightarrow 0} \frac{\sqrt{x^2 + b^2} - b}{x^2} &= \lim_{x \rightarrow 0} \left(\frac{\sqrt{x^2 + b^2} - b}{x^2} \right) \left(\frac{\sqrt{x^2 + b^2} + b}{\sqrt{x^2 + b^2} + b} \right) \\
 &= \lim_{x \rightarrow 0} \frac{(x^2 + b^2) - (b)^2}{x^2 (\sqrt{x^2 + b^2} + b)} = \lim_{x \rightarrow 0} \frac{x^2}{x^2 (\sqrt{x^2 + b^2} + b)} \\
 &= \lim_{x \rightarrow 0} \frac{1}{\sqrt{x^2 + b^2} + b} = \frac{1}{\sqrt{(0)^2 + b^2} + b} = \frac{1}{\sqrt{b^2} + b} = \frac{1}{b + b} = \frac{1}{2b}
 \end{aligned}$$

$$\begin{aligned}
 38) \lim_{t \rightarrow 0} \left(\frac{1}{t} - \frac{1}{t^2 + t} \right) &= \lim_{t \rightarrow 0} \left(\frac{1}{t} - \frac{1}{t(t+1)} \right) \quad \text{LCD} = t(t+1) \\
 &= \lim_{t \rightarrow 0} \frac{1(t+1) - 1}{t(t+1)} = \lim_{t \rightarrow 0} \frac{t}{t(t+1)} = \lim_{t \rightarrow 0} \frac{1}{t+1} = \frac{1}{(0)+1} = \frac{1}{1} = \underline{1}
 \end{aligned}$$

44) a) $\lim_{x \rightarrow 0} f(x) = \underline{3}$

b) $\lim_{x \rightarrow 3^-} f(x) = \underline{4}$

c) $\lim_{x \rightarrow 3^+} f(x) = \underline{2}$

d) $4 = \lim_{x \rightarrow 3^-} f(x) \neq \lim_{x \rightarrow 3^+} f(x) = 2$

e) $f(3) = \underline{3}$

$\lim_{x \rightarrow 3} f(x) : \underline{\text{D.N.E.}}$, "does not exist"

48) $f(t) = \begin{cases} t^2 & \text{if } t < 0 \\ e^t & \text{if } t \geq 0 \end{cases}$

a) i) $\lim_{t \rightarrow -1} f(t) = \lim_{t \rightarrow -1} t^2 = (-1)^2 = \underline{1}$

ii) $\lim_{t \rightarrow 0^-} f(t) = \lim_{t \rightarrow 0^-} t^2 = (0^-)^2 = 0^- = \underline{0}$

48) continued

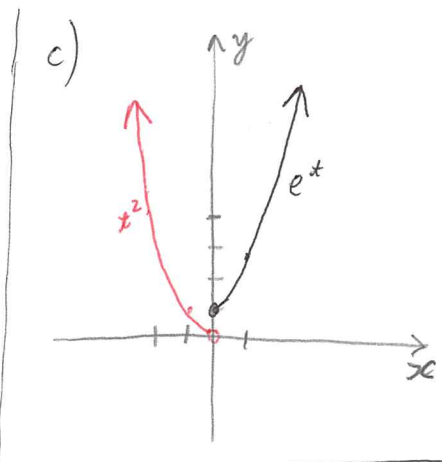
$$iii) \lim_{t \rightarrow 0^+} f(t) = \lim_{t \rightarrow 0^+} e^t = e^{(0^+)} = e^{(0)} = \underline{\underline{1}}$$

$$iv) \lim_{t \rightarrow 0} f(t) : DNE \text{ because } 0 = \lim_{t \rightarrow 0^-} f(t) \neq \lim_{t \rightarrow 0^+} f(t)$$

$$v) \lim_{t \rightarrow 2} f(t) = \lim_{t \rightarrow 2} e^t = e^{(2)} = \underline{\underline{e^2}}$$

b) f is not continuous at $t=0$ because

$$\lim_{t \rightarrow 0^-} f(t) \neq f(0) = \lim_{t \rightarrow 0^+} f(t)$$



$$50) F(x) = \frac{x^2 - 1}{|x - 1|}$$

$$a) i) \lim_{x \rightarrow 1^+} F(x) = \lim_{x \rightarrow 1^+} \frac{x^2 - 1}{|x - 1|} = \lim_{x \rightarrow 1^+} \frac{x^2 - 1}{+(x - 1)} = \lim_{x \rightarrow 1^+} \frac{(x+1)(x-1)}{(x-1)} = \lim_{x \rightarrow 1^+} (x+1) = ((1^+) + 1) = \underline{\underline{2}}$$

$$ii) \lim_{x \rightarrow 1^-} F(x) = \lim_{x \rightarrow 1^-} \frac{x^2 - 1}{|x - 1|} = \lim_{x \rightarrow 1^-} \frac{x^2 - 1}{-(x - 1)} = \lim_{x \rightarrow 1^-} \frac{(x+1)(x-1)}{(-1)(x-1)} = \lim_{x \rightarrow 1^-} \frac{(x+1)}{(-1)} = \frac{((1^-) + 1)}{(-1)} = \frac{2}{-1} = \underline{\underline{-2}}$$

b) $\lim_{x \rightarrow 1} F(x) DNE$

because

$$-2 = \lim_{x \rightarrow 1^-} F(x) \neq \lim_{x \rightarrow 1^+} F(x) = 2$$

c)

