## Name:

Note that both sides of each page may have printed material.


## Instructions:

1. Read the instructions.
2. Do this test on your own after studying. It should take you $\mathbf{1}$ hour and $\mathbf{2 0}$ minutes. Cheating will make your life harder, as if you do it, the final will destroy you and a good grade here won't matter.
3. IMPORTANT: All closed surfaces in this exam are positively oriented.
4. Print out this exam, staple it, and write your full solutions on it in the appropriate spaces.
5. Bring your completed exam to the class on the date above. No extensions or excuses allowed!
6. Complete all problems in the actual test. Bonus problems are optional and will only be counted if all other problems are attempted. All non-bonus problems are equally weighted.
7. Show ALL your work to receive full credit, unless otherwise stated. You will get 0 credit for simply writing down the answers.
8. Write neatly so that I am able to follow your sequence of steps and box your answers.
9. Read through the exam and complete the problems that are easy (for you) first!
10. You are NOT allowed to use notes, or other aids-including, but not limited to, divine intervention/inspiration, the internet, telepathy, knowledge osmosis, the smart kid that may be sitting beside you or that friend you might be thinking of texting.
11. Write exact answers only. NOT decimal approximations.
12. Use the correct notation and write what you mean! $x^{2}$ and $x 2$ are not the same thing, for example, and I will grade accordingly.
13. Other than that, have fun and good luck!
when jhevon makes test 2 take home givin me a chance to drastically improve my grade

14. Let $C$ be the curve of intersection of $z=\sqrt{x^{2}+y^{2}}$ and the plane $z=3$. Let $\vec{F}=\left\langle 3 y, x^{3} / 3, e^{z}\right\rangle$. Compute $\oint_{C} \vec{F} \cdot d \vec{r}$ in two ways:
(a) Directly as a line integral. (10 points)
(This is problem 1 recopied for your convenience. Do part (b) on this page!)
Let $C$ be the curve of intersection of $z=\sqrt{x^{2}+y^{2}}$ and the plane $z=3$. Let $\vec{F}=\left\langle 3 y, x^{3} / 3, e^{z}\right\rangle$.
Compute $\oint_{C} \vec{F} \cdot d \vec{r}$ in two ways:
(b) As a double integral using Stokes' Theorem. (10 points)
15. Let $E$ be the solid region bounded by $z=9-\sqrt{x^{2}+y^{2}}$ and the $x y$-plane. Let $S$ be the two-part boundary of $E$. If $\vec{F}=\langle x, y,-z\rangle$, compute the total flux over $E$ in two ways:
(a) Directly as a surface integral. (10 points)
(This is problem 2 recopied for your convenience. Do part (b) on this page!)
Let $E$ be the solid region bounded by $z=9-\sqrt{x^{2}+y^{2}}$ and the $x y$-plane. Let $S$ be the two-part boundary of $E$. If $\vec{F}=\langle x, y,-z\rangle$, compute the total flux over $E$ in two ways:
(b) As a triple integral using the Divergence Theorem. (10 points)
me and my GPA livin' our best lives

jhevon's class


DRACARYS
3. (a) (10 points) Find the reduced row-echelon form of:

$$
\left(\begin{array}{cccc}
1 & 1 & 2 & 2 \\
1 & 0 & 1 & -1 \\
2 & 1 & 3 & 1
\end{array}\right)
$$

(b) (5 points) Hence, find the solution to the system: $\left\{\begin{aligned} x+y+2 z & = \\ x & +z= \\ 2 x+y+3 z & =\end{aligned}\right\}$. Write your solution as a sum of column vectors if applicable.
4. Let $A=\left(\begin{array}{ccc}1 & 4 & 1 \\ 0 & 4 & 1 \\ 2 & 10 & 2\end{array}\right)$.
(a) (10 points) Find the inverse of $A$.
(b) (5 points) Use your answer to part (a) to solve the system

$$
\begin{array}{r}
x+4 y+z=1 \\
2 x+4 y+z=1 \\
2 x+2 z=0
\end{array}
$$

5. Let $A=\left(\begin{array}{ccc}1 & 4 & 1 \\ 0 & 4 & 1 \\ 2 & 10 & 2\end{array}\right)$.
(a) (10 points) Compute: (i) $\operatorname{det} A$, (ii) $\operatorname{det} A^{-1}$, (iii) $\operatorname{det}\left(2 A^{3} A^{T} A^{-2}\right)$.
(b) (5 points) Use Cramer's Rule to solve for $x$ only (do not solve for $y$ or $z!!!$ ) in the following system. No credit for any other method.

$$
\begin{aligned}
x+4 y+z & =1 \\
4 y+z & =1 \\
2 x+10 y+2 z & =0
\end{aligned}
$$

6. Let $A=\left(\begin{array}{ll}2 & 3 \\ 4 & 3\end{array}\right)$.
(a) (10 points) Find the eigenvalues and corresponding eigenvectors of $A$. Indicate which vectors correspond with which values using appropriate notation.
(b) (5 points) Use your answer in part (a) to find the general solution to the system

$$
\begin{aligned}
y_{1}{ }^{\prime} & =2 y_{1}+3 y_{2} \\
y_{2}{ }^{\prime} & =4 y_{1}+3 y_{2}
\end{aligned}
$$

Bonus Problems: Note that you must attempt all problems in the actual test to be eligible to attempt the bonus problems. Otherwise, anything you write on this page will be disregarded.

1. Let $A$ be the matrix in problem 6. Diagonalize $A$ by finding an invertible matrix $P$ and a diagonal matrix $D$ such that $A=P D P^{-1}$ (5 points).
2. Let $A$ be as in problem 1 above. Compute $A^{6}$ as a $2 \times 2$ matrix ( 5 points).
3. Let $\vec{F}=<4 y, x, 2(2 y-x)>$. Find $\int_{C} \vec{F} \cdot d \vec{r}$ where $C$ is the circle of radius 3 in the plane $x-y+z=2$ centered at $(2,2,2)$ and oriented clockwise when viewed from the origin ( 5 points).
mrw jhevon says we have a take home test

me after taking the take home test

