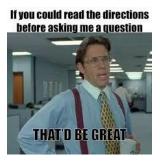
March 27, 2019

Name: _____

Note that both sides of each page may have printed material.



Instructions:

- 1. Read the instructions.
- 2. Panic!!! Kidding, don't panic! I repeat, do NOT panic! Don't look down, while you're at it.
- 3. Complete all problems.
- 4. Show **ALL** your work to receive full credit, unless otherwise stated. You will get 0 credit for simply writing down the answers.
- 5. Write neatly so that I am able to follow your sequence of steps and box your answers.
- 6. Read through the exam and complete the problems that are easy (for you) first!
- 7. You are NOT allowed to use notes, or other aids—including, but not limited to, divine intervention/inspiration, the internet, telepathy, knowledge osmosis, the smart kid that may be sitting beside you or that friend you might be thinking of texting.
- 8. In fact, cell phones and watches should be out of sight! If I catch you with a cellphone or a watch, you will fail the exam. If I catch you with any other paper than this exam, you will fail the exam. No calculators.
- 9. Use the correct notation and write what you mean! x^2 and x^2 are not the same thing, for example, and I will grade accordingly.
- 10. Other than that, have fun and good luck!



You're gonna pass this test

'cuz I dunno what Imma do if I don't

- 1. Let $F = \langle 3x^2, \frac{z^2}{y}, 2z \ln y \rangle$.
- (a) Show that F is conservative by finding a potential function, f, for F. (15 points)

(b) Find the work done by ${\it F}$ in moving an object along the path ${\it C}$, where ${\it C}$ is parametrized by two curves: the vector curve $\vec{r}(t) = \langle e^{t^2}, t+1, \sin t \rangle$ from (1,1,0) to $(e,2,\sin 1)$ (Note that t=0 for the first point and t=1 for the second point), followed by the straight line segment from $(e,2,\sin 1)$ to (0,1,1) (Remember how to parametrize line segments and how to set up the limits!!!). (5 points)

2. Compute $\int_C x + \sqrt{y} \, ds$, where C is the closed curve in the plane consisting of a parabolic arc along $y = x^2$ from (0,0) to (1,1), followed by a line segment from (1,1) back to (0,0). Include a sketch of C in your answer. (20 points)

3. Let S be the part of the surface $z=1-x^2$ in the first octant with $0 \le y \le 1$. Let C be the curve of intersection of S with the plane y=1. If $F=<x^2$, y^3 , 3>, find the work done by F in moving a particle along the curve C; assuming C is oriented so that the final point is in the xy-plane. (20 points)

4. Let R be the region in the second quadrant bounded by the circle of radius a, y = 0, and x = 0. Let C be the boundary curve of R, oriented *counter-clockwise*.

Compute
$$\oint_C -xy \, dx + xy \, dy$$
 in two ways:

(a) Directly as a line integral. (10 points)

(This is problem 4 recopied for your convenience. Do part (b) on this page!)

Let R be the region in the second quadrant bounded by the circle of radius a, y=0, and x=0. Let C be the boundary curve of R, oriented *counter-clockwise*.

Compute
$$\oint_C -xy \, dx + xy \, dy$$
 in two ways:

(b) As a double integral using Green's Theorem. (10 points)

5. Compute $\iint_S x \, dS$, where S is the portion of $z = x^2 + y^2$ in the first octant for $z \le 4$ (10 points)

- 6. Let $\vec{F} = \langle x \sin y, y \ln z, xyz \rangle$. Compute (5 points each):
- (a) $\operatorname{curl} \vec{F}$

(b) $\operatorname{div} \vec{F}$



