Math 392 Test 1A February 27, 2018

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Note that both sides of each page may have printed material.

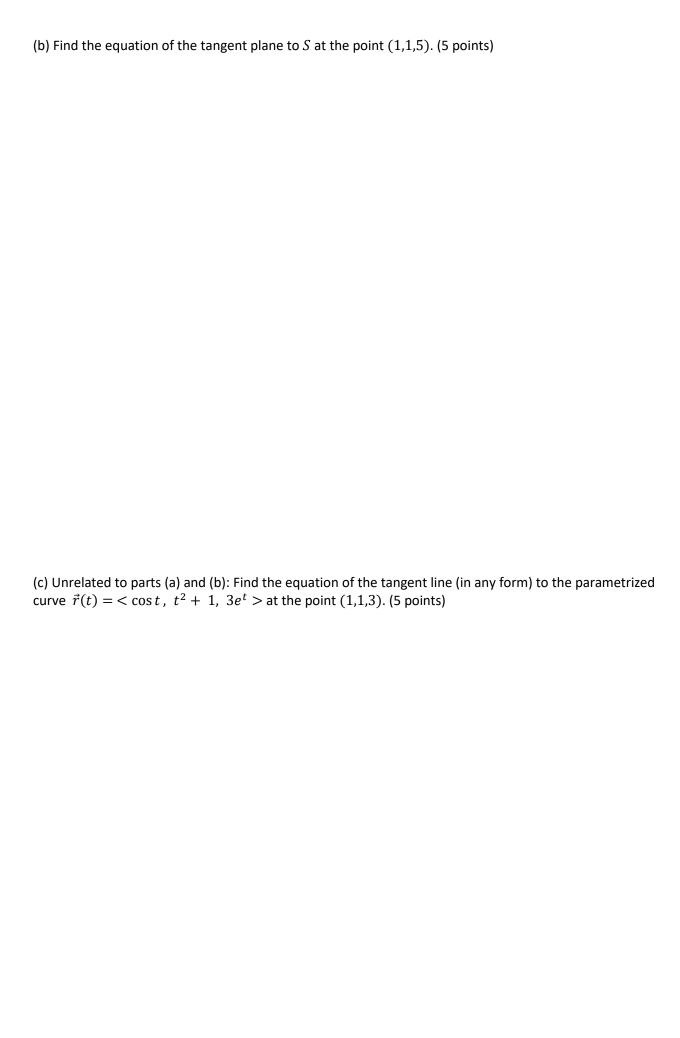
Instructions:

- Read the instructions.
- 2. Panic!!! Kidding, don't panic! I repeat, do NOT panic! Don't look down, while you're at it.
- 3. Complete all problems in the actual test. Bonus problems are, of course, optional. And they will only be counted if all other problems are attempted.
- 4. Show ALL your work to receive full credit. You will get 0 credit for simply writing down the answers.
- 5. Write neatly so that I am able to follow your sequence of steps and box your answers.
- 6. Read through the exam and complete the problems that are easy (for you) first!
- 7. No calculators, notes or other aids allowed! Including, but not limited to, divine intervention/inspiration, the internet, telepathy, knowledge osmosis, the smart kid that may be sitting beside you or that friend you might be thinking of texting.
- 8. In fact, cell phones should be out of sight!
- 9. Use the correct notation and write what you mean! x^2 and x^2 are not the same thing, for example, and I will grade accordingly.
- 10. Don't commit any of the blasphemies mentioned in the syllabus!
- 11. Other than that, have fun and good luck!

May the force be with you. But you can't ask it to help you with your test.



- 1. Let S be the part of the surface $z=9-2x^2-2y^2$ between the planes z=1 and z=5 in the first octant.
- (a) Compute the surface area of S. (10 points)



- 2. Let $F = \langle yze^{xy} + y \sin z, xze^{xy} + x, e^{xy} x\cos z \rangle$.
- (a) Show that F is conservative by finding a potential function, f, for F. (15 points)

(b) Find the work done by ${\it F}$ in moving an object along the path ${\it C}$, where ${\it C}$ is parametrized by two curves: the vector curve $\vec{r}(t) = \langle e^{t^2}, t+1, \sin t \rangle$ from (1,1,0) to $(e,2,\sin 1)$ (Note that t=0 for the first point and t=1 for the second point), followed by the straight line segment from $(e,2,\sin 1)$ to (0,0,1) (Remember how to parametrize line segments and how to set up the limits!!!). (5 points)

3. Compute $\int_C x^2 + 1 \, ds$, where C is the three-quarter circle $x^2 + y^2 = 1$ from (1,0) to (0,-1) followed by the line segment from (0,-1) to (0,-2). (20 points)

4. Let R be the region bounded by the upper semi-circle $x^2 + y^2 = 4$ and the line y = 0. Let C be the boundary of R oriented *clockwise*.

Compute $\oint_C 3y \, dx - 2x \, dy$ directly as a line integral. Include a sketch of the region in your answer. (20 points)

5. Let S be the part of the surface $z=1-x^2$ in the first octant with $0 \le y \le 2$. Let C be the curve of intersection of S with the plane y=0. If F=<1, y, $x^2>$, find $\int_C F\cdot dF$. (C is oriented so that the final point is in the xy-plane). (20 points)

Bonus Problems: Note that you must complete all problems in the actual test to be eligible to attempt the bonus problems. Otherwise, anything you write on this page will be disregarded.

1. Verify your answer in problem 4. by using Green's Theorem. (5 points)

2. Compute the arclength along $\vec{r}(t) = \langle t^2, 2t, \ln t \rangle$ from the point (1,2,0) to (e^2 , 2e, 1). (5 points)

3. Let $F = \langle x^2yz, xy^2z, xyz^2 \rangle$. Compute (5 points each):

(a) ${
m curl} \vec{F}$

(b) $\operatorname{div} \vec{F}$

