Math 392 Quiz 7B

March 11, 2019

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Instructions: No calculators! Answer <u>all</u> problems in the space provided! Do your rough work on scrap paper.

Define the following:

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(a)
$$\int_{C} f(x,y) dy = \frac{\int_{a}^{b} f(x(t),y(t)) y'(t) dt}{\int_{c}^{b} f(x(t),y(t)) \cdot \vec{r}'(t) dt}$$

(b)
$$\int_{C} \vec{r} \cdot d\vec{r} = \frac{\int_{a}^{b} \vec{r} \cdot (\vec{r}(t)) \cdot \vec{r}'(t) dt}{\int_{c}^{b} f(x(t)) \cdot \vec{r}'(t) dt}$$

(c)
$$\int_{C} f(x,y) ds = \int_{a}^{b} \int_{a}^{b} (x(t), y(t)) \sqrt{(x'(t))^{2} + (y'(t))^{2}} dt$$

(where C is a smooth curve parametrized by $\vec{r}(t) = \langle x(t), y(t) \rangle$. No shorthand, flesh out full definition.)

- What does it mean to say " \vec{F} is conservative"?
- State the equation in Green's Theorem:
- State the equation in the fundamental theorem for line integrals: $\int_{\mathcal{C}} \nabla f \cdot d\vec{r} = f(\vec{r}(b))$
- If $curl\vec{F} = \vec{0}$, then \vec{F} is called $\underline{\Gamma}$
- Let $\vec{F} = \langle P(x,y), Q(x,y) \rangle$ be defined on an open, simply connected domain D. Suppose P and Q have continuous first partial derivatives on D. What equation would you use to check if \vec{F} is conservative?
- 7. Let $\vec{F} = \langle P(x,y), Q(x,y), R(x,y) \rangle$ be defined on an open, simply connected domain D. Suppose P, Q, and R have continuous first partial derivatives on D. What equation would you use to check if \vec{F} is conservative?
- 8. Let $\vec{F} = \langle y \cos x, xy^3 e^z, x \tan(yz) \rangle$, compute:

(a)
$$curl\vec{F} = \frac{\langle xzsec^2(yz) - xy^3e^2, -tan(yz), y^3e^2 - \cos x \rangle}{2\pi^2}$$

(b)
$$\operatorname{div} \vec{F} = -y \sin x + 3xy^2 e^2 + xy \operatorname{Sec}^2(yz)$$