CWER S

Instructions: No calculators! Answer all problems in the space provided!

For a function f(x, y), write the formula for the tangent plane at (x_0, y_0) . You may use " f_x " instead of " $f_x(x_0, y_0)$ " and " f_v " instead of " $f_v(x_0, y_0)$ ".

 $\overline{Z} - \overline{Z}_o = f_X (X - X_o) + f_Y (Y - Y_o)$ For a function f(x, y), define, using limits, $\frac{\partial f}{\partial y} = f_y = \lim_{N \to 0} \frac{f(x, y+N) - f(x, y)}{N}$

- 3. Find the equation of the tangent plane to the function $f(x,y) = 2y + 2x^2y^3 4x^2y$ at the point where x = 2 and y = 1.

Z+6=-8(x-2)+10(y-1)

4. Find the indicated partial derivatives of $f(x, y, z) = y^x + xe^{-z} \cos y$

(a) $f_x = y^* \ln y + e^{-\frac{1}{2}} \cos y$ (b) $f_y = xy^{*-1} - xe^{-\frac{1}{2}} \sin y$ (c) $f_{xx} = \frac{y^{\times}(\ln y)}{(\ln y)^{-1}}$ (d) $\frac{\partial^2 f}{\partial x \partial y} = \frac{y^{\times - 1} + xy^{\times - 1} \ln y - e^{-\frac{y}{2}} \sin y}{(\ln y)^{-1}}$

Use differentials to estimate the amount of metal in a closed cylindrical can that is 10cm high and 4cm in diameter if the metal in the top and bottom is 0.2cm thick and the metal in the sides is 0.05 cm thick.

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6. What is the formula for the linearization of f(x, y) at the point (a, b)? You may use the shorthand described in 1.

 $L(x,y) = f(a,b) + f_x(x-a) + f_y(y-b)$

7. Let $f(x,y) = \sqrt{x^2 + y^2}$. Use linearization (or differentials) to approximate f(3.1,4.1). $f(3.1.4.1) \approx 5 + \frac{7}{50} = \frac{257}{50}$

Bonus Problems:

1. Suppose
$$z = f(x, y), x = x(s, t)$$
 and $y = y(s, t)$: $\frac{dz}{ds} = \frac{\partial f}{\partial x} \frac{\partial x}{\partial s} + \frac{\partial f}{\partial y} \frac{\partial y}{\partial s}$ (instead of "f")

Let F(x, y, z) = 0 be an implicitly defined function. $\frac{dz}{dy} = \frac{-+y}{-+y}$