Name

Instructions: No calculators! Answer all problems in the space provided! Do your rough work on scrap paper.

1. Complete the following rules:

(a)
$$x^n \cdot x^m =$$
 _____ (b) $x^{-a} =$ _____ (c) $x^{m/n} =$ _____ (d) $\frac{x^n}{x^m} =$ _____

(e)
$$x^2 - y^2 =$$
 ______(f) $x^3 - y^3 =$ _____

2. Reduce and simplify the following rational expressions:

(a)
$$\frac{x^6 - 64}{x^2 - 4} =$$
 ______(b) $\frac{250a + 100ax + 10ax^2}{50a - 2ax^2} =$ _____

(c)
$$\frac{ad-ad^2}{d-1} =$$
 ______ (d) $\frac{42x^2+23x-10}{14x^2+45x-14} =$ ______

(e)
$$\frac{28x^3y^5 + 42x^4y^3}{7x^2y^2} = \underline{\hspace{1cm}}$$

3. Combine and simplify the following rational expressions:

(a)
$$\frac{3a^2 + 7ab - 20b^2}{a^2 + 5ab + 4b^2} \div \frac{3a^2 - 17ab + 20b^2}{3a - 12b} = \underline{\qquad} (b) \frac{2x - 4}{x + 2} - \frac{x - 6}{x + 2} = \underline{\qquad}$$

(c)
$$5 - \frac{x}{2x+1} =$$
 _____ (d) $2 + \frac{1}{x} + \frac{x}{3x+9} - \frac{3}{x^2+3x} =$ _____

(e)
$$\frac{4-\frac{1}{x^2}}{4-\frac{4}{x}+\frac{1}{x^2}} =$$

Bonus (after attempting the problems above, do these for extra credit):

1. Combine:
$$\left(1 + \frac{2}{x+1}\right)\left(1 + \frac{2}{x+3}\right)\left(1 + \frac{2}{x+5}\right)\left(1 + \frac{2}{x+7}\right) =$$

2. Solve for
$$x: \frac{x}{x-2} + \frac{2}{3} = \frac{2}{x-2} \implies x =$$
